Basic Science Department Academic year: 2013 / 2014 Mathematics II Code: Math 102 Semester: Autumn Final Exam: January, 2014 Examiner: Dr. Mohamed Eid Time Allowed: 2 hours **Answer All questions** Total Mark 40 Faculty of Engineering ممنوع إستخدام المحمول كألة حاسبة. يُسمح فقط بإستخدام الألة الحاسبة العادية Do not use Mobile as Calculator. Only use regular Calculator Question 1 (a) If $A = \begin{bmatrix} 1 & 3 & 0 \\ 2 & 1 & -2 \end{bmatrix}$ and $B = \begin{bmatrix} 2 & -1 \\ 1 & 1 \\ 4 & 2 \end{bmatrix}$ 6 Find, if possible, A + B, $A.B^{t}$, $A + B^{t}$, BA, |A.B|(b) Find the eigenvalues and the eigenvectors of the matrix $A = \begin{bmatrix} 2 & 3 \\ 1 & 0 \end{bmatrix}$. 4 (c) Determine the type of solution of the linear system: 4 x + y + z = 5, x - y + 2z = 2, 2x + 3z = 5. Question 2 (a) Using the binomial theorem, expand $\frac{1}{3-2r}$ 2 (b) Find S_n , S_{10} from the series: (i) $\sum_{r=1}^{n} \frac{1}{r^2 \perp r}$ (ii) $\sum_{r=1}^{n} 2r(r^2 + 1)$ 4 **Ouestion 3** (a)State the definition hyperbola. 2 (b) Write the equation of circle where (2, -3), (1, 2) are ends of diameter. 2 (c) Find the angle between the lines and separate them $x^2 + xy - 2y^2 = 0$. 3 (d)Determine the vertex, focus and sketch the parabola $x^2 - 4x + 8y - 12 = 0$. 3 **Question 4** (a) Find center, vertices and sketch the ellipse: $x^2 + 4y^2 - 4x - 8y + 4 = 0$ 4 (b) Determine the type of the curve: $2x^2 - 3xy + 2y^2 - 16 = 0$ 4

Good luck

(i) $x^2 + y^2 + z^2 + 4x - 5 = 0$

(c)State the type of surface:

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(ii) $x^2 + (z - 2)^2 = (y - 3)^2$

2

Basic Science Department

Math. 2 Code: Math 102

Mid-Term Exam: November, 2013

Time Allowed: 60 Minutes



Academic year: 2013 / 2014

Semester: Autumn

Examiner: Dr. Mohamed Eid

Answer All questions

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[1] If
$$A = \begin{bmatrix} 0 & 2 \\ 1 & 3 \\ 2 & 1 \end{bmatrix}$$
 and $B = \begin{bmatrix} 2 & 1 & -2 \\ 1 & 0 & 3 \end{bmatrix}$

8

6

8

Total Mark: 30

Find, if possible, A + B, $A + B^{t}$, |A|, $|A.A^{t}|$, and |BA|.

- [2] Find the eigenvalues and the eigenvectors of the matrix $A = \begin{bmatrix} 2 & 4 \\ 1 & 2 \end{bmatrix}$.
- [3] Write the following equations in matrix form and determine the type of solution : x y + z = 1, 2x + y = 4, 3x + z = 6.
- [4] Using the binomial theorem, expand: $\frac{1}{\sqrt[3]{8-2x}}$.
- [5] Find S_n , S_{10} from the series:

(a)
$$\sum_{r=1}^{n} \frac{1}{r^2 + 3r + 2}$$

(b)
$$\sum_{r=1}^{n} 3r(r+4)$$

Good luck

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